

1 Mushu

1. Consider the `Tree` class below. Suppose we would like to write a method for this `Tree` class, `getAncestor(int k, Node target)`. This method takes in an integer k and a `Node target`, and returns the k 'th ancestor of `target` in our tree (you may assume such an ancestor exists). You may also assume that $k \geq 0$, that `target != null`, and that there are no cycles in our tree before we call this method.

```
1  public class Tree<T> {
2      private Node root;
3
4      private class Node{
5          public T item;
6          public ArrayList<Node> children;
7      }
8
9      public Node getAncestor(int k, Node target) {
10         List<Node> list = _____;
11         ancestorHelper(_____, _____, _____);
12         return list.get(_____);
13     }
14     private boolean ancestorHelper(_____, _____, _____) {
15         _____;
16         if (_____) {
17             return true;
18         }
19         for (_____) {
20             if (_____)
21                 return true;
22         }
23         _____;
24         return false;
25     }
26 }
27
```

2. Give a bound on the runtime of `getAncestor(int k, Node target)` in the best and worst cases in $\Theta(\cdot)$ notation in terms of N and k , for a tree with N nodes. How does our choice of list implementation on line 10 affect our runtime?

2 Kontakte

We're going to make our own Contacts application! The application must perform two operations: `addName(String name)`, which stores a new contact, and `countPartial(String partial)`, which returns the number of contacts whose names begin with `partial`. Implement both of these methods in the `Contacts` class below. You may find the work already done in the private `Node` class, as well as the method `String::charAt(int index)` useful.

```

1      public class Contacts {
2
3          private class Node {
4              public int _____;
5              public Map<Character, Node> children;
6
7              public Node() {
8                  _____;
9                  children = new HashMap<Character, Node>()
10             }
11
12             Node root;
13
14             public Contacts() {root = new Node();}
15
16             public void addName(String name) {
17                 Node current = root;
18                 for (_____; _____; _____) {
19                     if (_____) {
20                         Node n = new Node();
21                         _____;
22                     }
23                     _____;
24                     _____;
25                 }
26             }
27             public int countPartial(String partial) {
28                 Node current = root;
29                 for(_____; _____; _____) {
30                     if(_____) {
31                         _____;
32                     }
33                     else {return 0;}
34                 }
35                 return _____;
36             }
37         }
38     }

```

3 KND Trees

A k -d tree is a binary tree where each node contains a point of dimension k . Our goal is to create a tree of points which, when given a k -dimensional coordinate, can find the point closest to that coordinate (i.e. "what is the closest point to (a, b) ?").

Each node also has a splitting plane, which is one of these k dimensions. Say a node n has splitting plane x . Then everything to the left of n will have an x -coordinate less than or equal to n 's. Similarly, everything to the right of n will have an equal or greater x -coordinate. If n instead split on y , then the above holds for y -coordinates.

From the Wikipedia page for k -d trees, "As one moves down the tree, one cycles through the k axes used to select the splitting planes."

This means in a 3-dimensional tree:

- the root would have an x-aligned plane
- the roots children would both have y-aligned planes
- the roots grandchildren would all have z-aligned planes
- the roots great-grandchildren would all have x-aligned planes, etc.

1. Consider a 2-d tree in which the root splits on x . Normally, we want to turn a fixed set of points into a k -d Tree, and we don't have to worry about later additions. This makes it easier to make our Tree bushy. Discuss how you may do this efficiently, and draw a balanced k -d Tree of the points $(2, 3), (5, 4), (9, 6), (4, 7), (8, 1), (7, 2), (10, 10)$

2. What is the closest point in our tree to the coordinate $(3, 6)$? What about $(2, 5)$? What can you conclude about the worst-case runtime for closest point (otherwise known as nearest neighbor) search in a reasonably bushy k -d tree?